



## Article

# Numerical Investigations on the Transient Aerodynamic Performance Characterization of a Multibladed Vertical Axis Wind Turbine

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**Abstract:** The use of vertical axis wind turbines (VAWTs) in urban environments is on the rise due to their relatively smaller size, simpler design, lower manufacturing and maintenance costs, and above all, due to their omnidirectionality. The multibladed drag-based VAWT has been identified as a design configuration with superior aerodynamic performance. Numerous studies have been carried out in order to better understand the complex aerodynamic performance of multibladed VAWTs employing steady-state or quasi-steady numerical methods. The transient aerodynamics associated with a multibladed VAWT, especially the time–history of the power coefficient of each blade, has not been reported in the published literature. This information is important for the identification of individual blade’s orientation when producing negative torque. The current study aims to bridge this gap in the literature through real-time tracking of the rotor blade’s aerodynamic performance characteristics during one complete revolution. Numerical investigations were carried out using advanced computational fluid dynamics (CFD)-based techniques for a tip speed ratio of 0 to 1. The results indicate that transient aerodynamic characterization is 13% more accurate in predicting the power generation from the VAWT. While steady-state performance characterization indicates a negative power coefficient ( $C_p$ ) at  $\lambda = 0.65$ , transient analysis suggests that this happens at  $\lambda = 0.75$ .

**Keywords:** vertical axis wind turbine; computational fluid dynamics; transient performance characteristics; power coefficient



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## 1. Introduction

As the world transitions away from fossil fuels and carbon-based energy sources, the necessity of renewable energy is becoming increasingly paramount. In 2022, Scotland observed a record-high 35.3 TWh of renewable energy generation, of which the majority, 27.5 TWh, was a result of onshore and offshore wind [1]. Due to its lower cost, onshore wind is preferred, yet it is associated with a number of limitations. Traditional horizontal axis wind turbines (HAWTs) are large structures requiring sufficient installation space. This aspect is compounded by their lower capacity factor (typically between 25% and 35%) [2], as well as their requirement for a pitch control system. Especially in urban environments, HAWTs are not a feasible option and thus pave the way for adopting vertical axis wind turbines (VAWTs). VAWTs can operate at much lower wind speeds with high turbulence levels due to their lower startup torque and omnidirectionality [3], making them a suitable and commercially viable option in urban settings [4]. Moreover, their lower cut-in speed allows them to have enhanced aerodynamic performance in non-uniform wind environments where flow restrictions, such as buildings, create further air turbulence [5,6]. Meanwhile, due to their considerably smaller size compared to HAWTs, VAWTs have been

found to be ideal for low-power generation, suitable for domestic purposes such as space heating, etc.

VAWTs are typically of two types i.e., lift-based (or Darrieus) and drag-based (or Savonius) VAWTs. The aerodynamic performance characterization of lift-based VAWTs, both steady-state and transient, is readily available in the published literature [7–9]. However, the same cannot be said about drag-based VAWTs, where most of the studies have investigated the performance of conventional two-bladed S-rotor VAWTs [10,11]. Numerous studies have shown that the performance of a multibladed VAWT, having 12 rotor blades, is far superior to the conventional S-rotor VAWT [12–14]. However, most of these studies rely on steady-state performance characterization. The few studies that have employed transient models for multibladed VAWT performance characterization use the revolution-averaged approach. Although this is adequate for predicting overall power generation from the VAWT, it lacks an in-depth description of the aerodynamic behavior of individual blades during a complete rotation of the VAWT. Thus, this study is an attempt to bridge this knowledge gap.

The topic of negative torque/power generation from drag-based VAWTs is largely unexplored, especially in the context of multibladed VAWTs. Most of the studies carried out rely on steady-state aerodynamic performance characterization, which is computationally inexpensive but also inaccurate. Steady-state solvers predict the aerodynamic behavior of the VAWT at one particular orientation, which is the primary reason for inaccuracies in predicting VAWT  $C_p$  [13]. Similarly, in cases where there is complex terrain, such as hills, mountains, escarpments, and forests, which significantly impacts the dynamic behavior of the wind, and consequently the turbine's performance over time [15,16], a transient solver would be a better choice to accurately capture the complex flow dynamics. As reported by Liu et al. [17], failures in steady simulations from base conditions had to be user-altered, by rotating their test of cylindrical flow about its axis in order to begin the simulation. This was done to force the simulation to run as well as to reduce initialization deviations, thereby reducing computational power and simulation time. They later concluded that the numerical results of vortex shedding and various other parameters were impaired as a direct result of this initial interference.

It has been identified that transient aerodynamic performance evaluation of individual blades of multibladed VAWTs is beneficial for further development of the technology and its widespread adoption for urban conditions. In order to address this challenge, advanced CFD techniques were employed to a multibladed VAWT in order to obtain accurate aerodynamic performance. This study also examines the contributions of individual blades of this VAWT towards net power generation. This will help identify potential areas of design improvement, particularly for isolated use in low power-requiring environments.

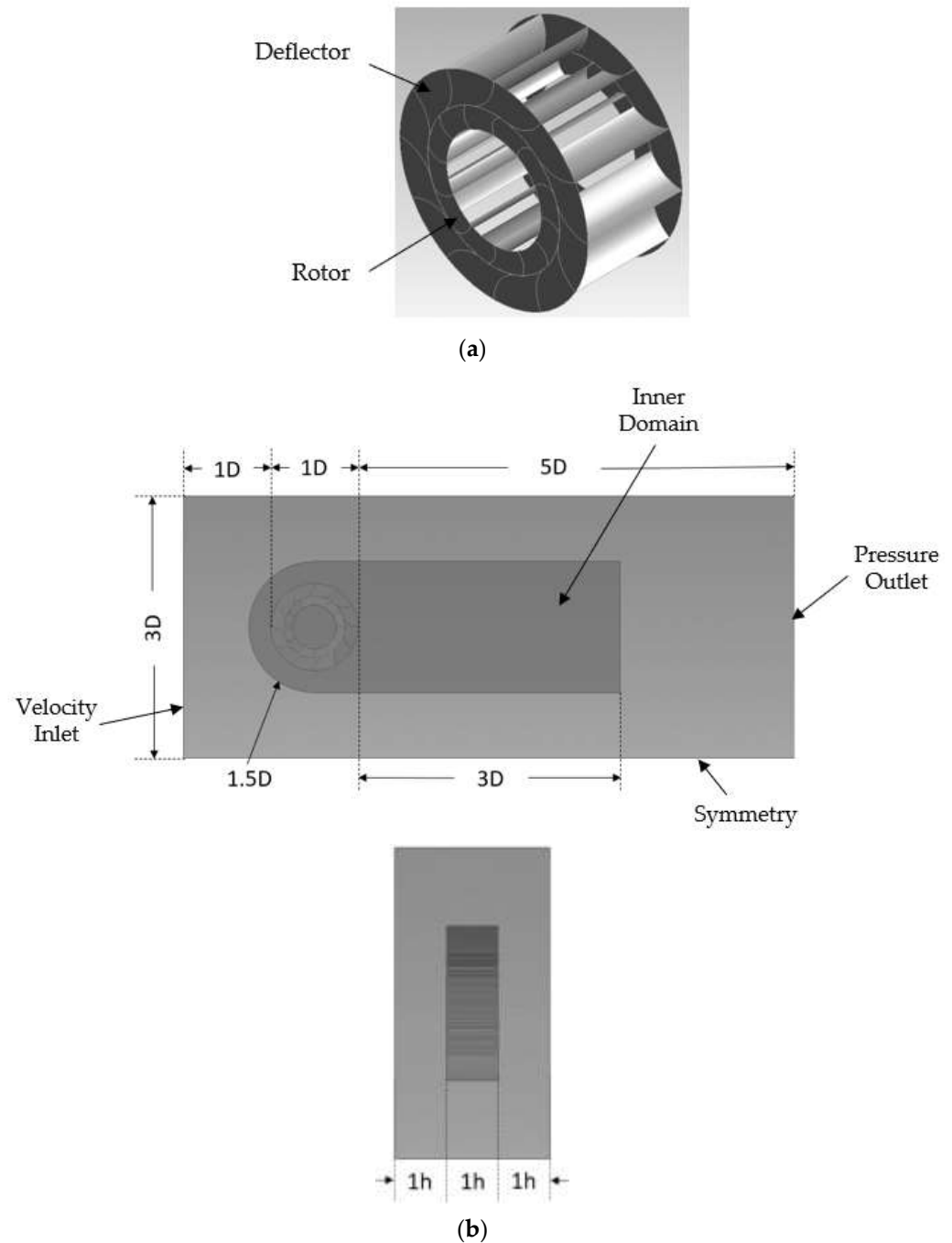
## 2. Numerical Modeling of the Multibladed VAWT

The computational fluid dynamics (CFD) solver was employed in the present study to numerically investigate the transient aerodynamic characteristics of the multibladed drag-based VAWT. The details of the numerical modeling techniques used in the present study, including the steps involved, are presented in the following sub-sections.

### 2.1. Geometry of the Multibladed VAWT and the Flow Domain

The design of the multibladed VAWT is based on [13] and comprises 12 rotor blades and 12 deflector blades, as shown in Figure 1a. The diameter of the rotor is 1.4 m while that of the deflector (D) is 2 m. The height of the VAWT (h) is 1 m. Figure 1b depicts the geometry of the flow domain. It can be seen that the flow domain is composed of two regions i.e., the inner region and the outer region. These regions have been created to control the mesh density and quality in the near-VAWT and far-VAWT regions, in accordance with the recommendations in the published literature [12,14]. The dimensions of the flow domain are such that the gap between the VAWT and the upstream boundary is kept constant at 1 D, while the downstream gap is 5 D. Similarly, in the spanwise direction, the gap between the

domain and the VAWTs is 1 h. These dimensions of the flow domain have been prescribed based on published numerical studies on multibladed VAWT [12,14].



**Figure 1.** (a) CAD model of the multibladed VAWT; (b) geometric details of the flow domain.

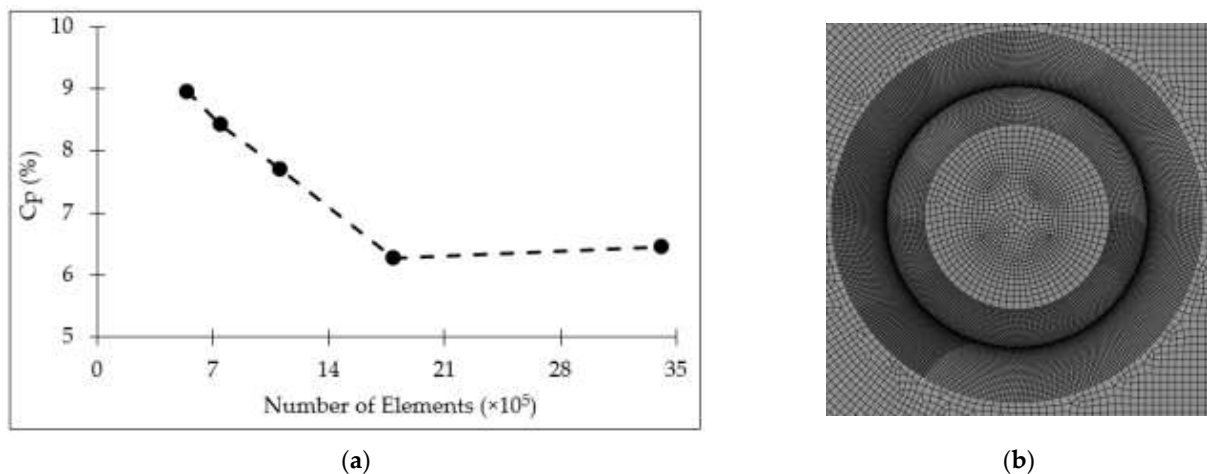
## 2.2. Meshing of the Flow Domain

Meshing of the flow domain was carried out in such a way that the mesh density was the finest (highest) in the flow channels between the rotor and deflector blades, while also ensuring that the mesh elements were structured, preferably quadrilateral, to minimize numerical errors. The mesh density in the core region of the VAWTs and the inner region of the flow domain was kept moderate, while it was coarsest in the outer region. For the purpose of the mesh independence study, five different element sizes were considered, as summarized in Table 1.

**Table 1.** Mesh sizing details for the flow domain.

Mesh	Element Size in the VAWT (mm)	Element Size in the Inner Region (mm)	Element Size in the Outer Region (mm)	Total Number of Mesh Elements ( $\times 10^5$ )
1 (coarsest)	8	24	100	5.41
2	7	21	100	7.42
3	6	18	100	11.01
4	5	15	100	17.89
5 (finest)	4	12	100	34.06

Figure 2a depicts the results of mesh independence testing of the multibladed VAWT. It can be seen that as the element size decreases (increasing the number of mesh elements), the numerically predicted power coefficient ( $C_p$ ) of the VAWT decreases till mesh #4 (comprising  $11.01 \times 10^5$  elements). Further decreasing the mesh size had an insignificant effect on the accuracy of the results and thus, mesh #4 was chosen to conduct the transient aerodynamic performance characterization of the VAWT in the present study. Figure 2b depicts mesh #4 in the vicinity of the multibladed VAWT.

**Figure 2.** (a) Mesh independence test results. (b) Mesh #4 for multibladed VAWT.

### 2.3. Boundary Conditions and Turbulence Modeling

Numerical investigations were carried out at 8 m/s wind speed, which is the average wind speed in Scotland. Thus, the upstream boundary of the flow domain was modeled as the inlet air velocity. The side walls of the flow domain were modeled symmetrically to mimic zero-shear slip walls, while the downstream boundary was modeled as a pressure outlet at 0 Pa,  $g$  to mimic the far-field.

The mass conservation equation solved within the flow domain is:

$$\frac{\partial}{\partial x_i}(u_i) = 0$$

where  $u_i$  is the flow velocity field. Momentum conservation/unsteady Reynolds-averaged Navier–Stokes (URANS) is:

$$\rho \frac{\partial}{\partial t}(u_i) + \frac{\partial}{\partial x_j}(u_i u_j) = -\frac{\partial P}{\partial x_i} + \mu \frac{\partial}{\partial x_j} \left( \frac{\partial u_i}{\partial x_j} \right) + \frac{\partial}{\partial x_j} (-\rho \overline{u_j u_i})$$

where  $\rho$  is the density of air =  $1.2 \text{ kg/m}^3$ ,  $\mu$  is the dynamic viscosity of air =  $1.789 \times 10^{-5} \text{ Pa.s}$ ,  $P$  is air pressure (Pa), and the term  $(-\rho \overline{u_j u_i})$  represents the Reynolds stress, which was modeled using the two-equation shear-stress transport (SST)  $k$ - $\omega$  turbulence model, developed by Menter [18]. The peculiarity of the SST  $k$ - $\omega$  model to behave as a standard  $k$ - $\omega$  model

in the near-wall regions (blades of the VAWT) with superior behavior in predicting wall shear, while behaving as a  $k$ - $\epsilon$  model away from the wall, makes it ideal for modeling air turbulence in the vicinity of the VAWT. The turbulent kinetic energy ( $k$ ) and the turbulence dissipation rate ( $\omega$ ) are modeled as:

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j} \left[ \sigma_k \frac{\partial k}{\partial x_j} \right] + G_k - D_k \quad (1)$$

$$\frac{\partial}{\partial t}(\rho \omega) + \frac{\partial}{\partial x_i}(\rho \omega u_i) = \frac{\partial}{\partial x_j} \left[ \sigma_\omega \frac{\partial \omega}{\partial x_j} \right] + G_\omega - D_\omega + Y_\omega \quad (2)$$

where  $\sigma$  represents effective diffusivity,  $G$  represents a generation,  $D$  represents dissipation, and  $Y$  represents cross-diffusion.

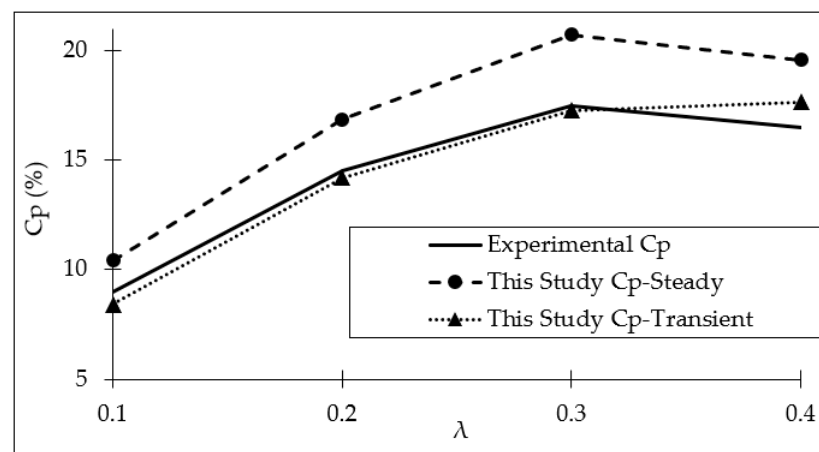
#### 2.4. Validation of the Numerical Model

In order to validate the numerical model developed here, experimental data from Colley [13] were used. Colley used the same VAWT model and calculated the  $C_p$  of the VAWT using wind tunnel tests at various tip speed ratios ( $\lambda$ ). The  $C_p$  and the  $\lambda$  were defined as:

$$C_p = \left( \frac{\omega T}{\frac{1}{2} \rho A V^3} \right) \times 100 \quad (3)$$

$$\lambda = \frac{\omega R}{V} \quad (4)$$

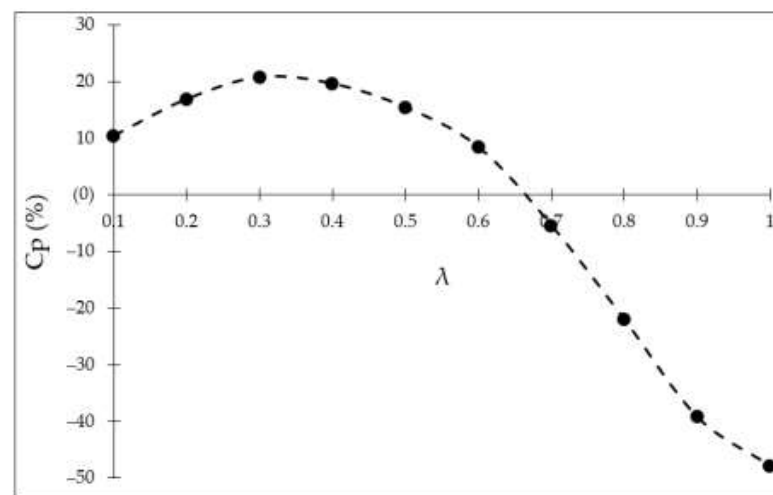
where  $\omega$  is the rotational velocity of the VAWT (rad/s),  $T$  is the torque applied by air on the VAWT (Nm),  $A$  is the projected area of the VAWT  $= 2 \times 1 = 2 \text{ m}^2$ ,  $V$  is the upstream air velocity  $= 8 \text{ m/s}$ , and  $R$  is the radius of the rotor  $= 0.7 \text{ m}$ . An important point to note here is that the wind tunnel used by Colley had a cross-section of  $600 \text{ mm} \times 600 \text{ mm}$  and thus, the incident airstream was directed towards one-half of the VAWT only. In order to validate the numerical model developed here, necessary modifications to the airflow inlet were made to ensure similarity in modeling. Figure 3 depicts the comparison between the experimental results of Colley and the numerical results of this study (both steady and revolution-averaged transient). Although the detailed results of this study are discussed in later sections, it can be clearly seen that the experimentally recorded  $C_p$  of the VAWT matches more closely to the revolution-averaged transient  $C_p$  rather than steady-state  $C_p$ . The average difference between experimental  $C_p$  and steady-state  $C_p$  is 17.3%, while between the experimental and revolution-averaged transient  $C_p$  is 4.3%, over the range considered here, i.e.,  $\lambda = 0.1$  to  $0.4$  (Colley presented results till  $\lambda = 0.4$ ).



**Figure 3.** Comparison of experimental measured and numerical predicted  $C_p$  of the multibladed VAWT.

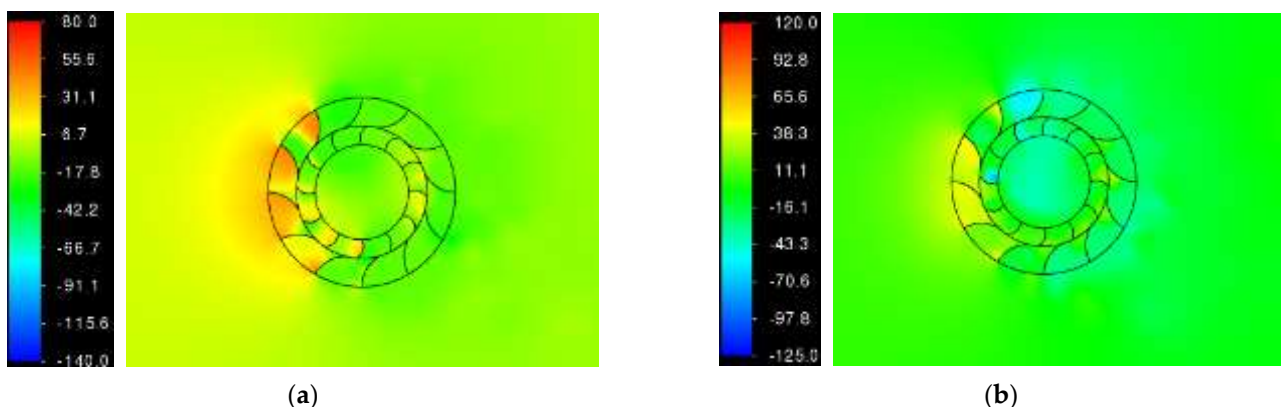
### 3. Steady-State Aerodynamic Characterization

Before moving on to the transient aerodynamic performance evaluation of the multi-bladed VAWT, it is beneficial to analyze its aerodynamic performance based on a steady-state solver, which will help highlight the advantages of transient formulation later on in this study. Multiple reference frame (MRF) modeling techniques were employed for this purpose. In the MRF technique, the rotation of blades is modeled through the application of rotational velocity components on the surface of the blades, while physically, the blades stay in the same orientation. Figure 4 depicts the variations in  $C_p$  against  $\lambda$  for the multi-bladed VAWT. It can be seen that as  $\lambda$  increases from 0.1 to 0.3,  $C_p$  also increases. At  $\lambda = 0.3$ , a peak  $C_p$  of 20% is achieved. Further increases in  $\lambda$  result in a decrease in  $C_p$ . At  $\lambda = 0.65$ , the  $C_p$  of the multi-bladed VAWT drops below 0. The positive  $C_p$  range of the multi-bladed VAWT is thus limited to  $\lambda = 0.3$ . From  $\lambda = 0.7$ , the decrease in  $C_p$  is almost linear. It should be noted that a conventional S-rotor VAWT with two blades and an aspect ratio of two, similar to the multi-bladed VAWT considered here, demonstrates a  $C_p$  of 6% at 8 m/s wind speed [19]. Thus, the multi-bladed VAWT considered here is far superior in extracting wind power than the conventional drag-based VAWTs.



**Figure 4.** Steady-state  $C_p$  variations in the multi-bladed VAWT.

Analyzing the flow fields associated with multi-bladed VAWT at peak and minimum  $C_p$  values, Figure 5 depicts static pressure variations in the vicinity of the VAWT at  $\lambda = 0.3$  (peak  $C_p$ ) in Figure 5a, and at  $\lambda = 1.0$  (minimum  $C_p$ ) in Figure 5b. It is clear that while operating at peak  $C_p$ , multi-bladed VAWT's windward rotor blades experience significant positive air pressure. While operating at minimum  $C_p$ , the same rotor blades experience significant negative air pressure, resulting in performance degradation of the VAWT.



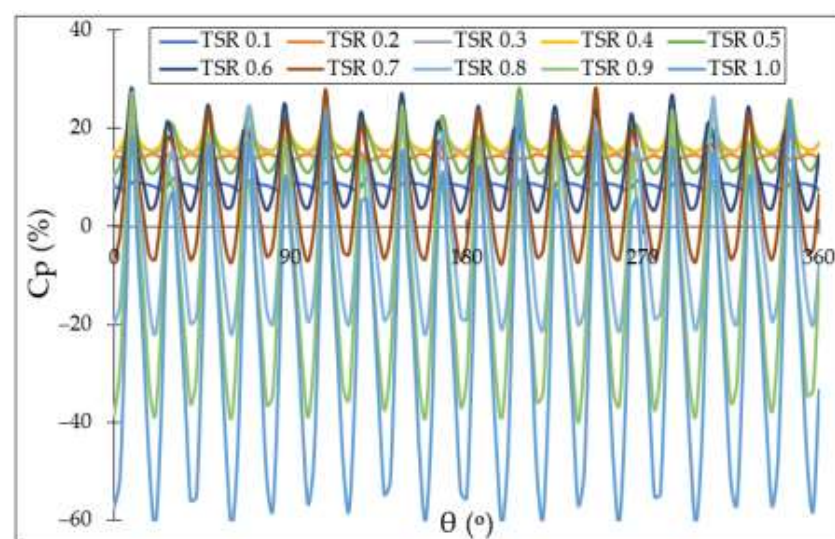
**Figure 5.** Static pressure variations at (a) peak  $C_p$  and (b) minimum  $C_p$  of the multi-bladed VAWT.



#### 4. Transient Aerodynamic Characterization

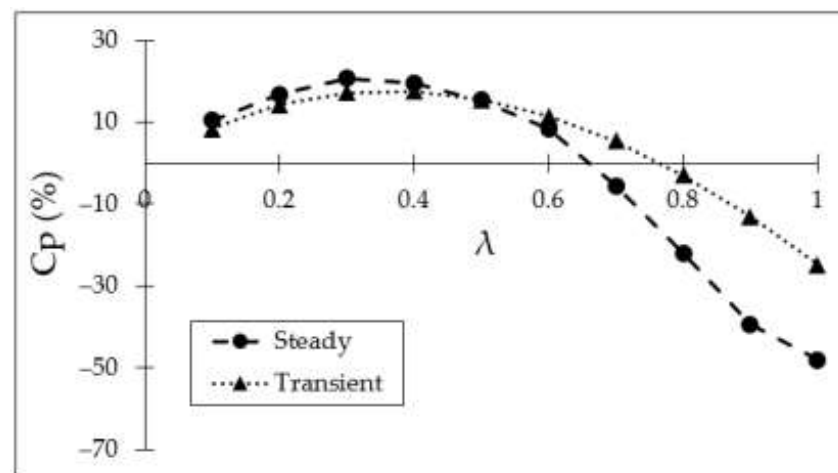
The use of steady-state techniques, such as MRF, is computationally inexpensive, and thus, results can be obtained quickly. Transient solvers are employed where the accuracy of the numerical predictions precedes computational expense. In the present study, the sliding mesh technique was employed to investigate the transient aerodynamic performance characteristics of the multibladed VAWT. In this technique, the rotor blades rotate physically, changing orientation with respect to space and time. For accurate numerical predictions and solver stability, the choice of time step size becomes important. Several published studies by the authors [4,12,14] have established that a time step size corresponding to a  $3^\circ$  rotation of the blades is capable of accurately predicting the aerodynamic performance of VAWTs with reasonable accuracy when turbulence in the flow domain is modeled using two-equation models like  $k-\epsilon$  or  $k-\omega$ . Thus, in the present study, a time step size of a  $3^\circ$  rotation of the blades was used.

In order to analyze the transient aerodynamic performance characteristics of VAWTs, their power coefficient and static pressure fields were chosen for analysis, as in Section 3. While steady-state solvers consider a single time step, resulting in a single  $C_p$  value for the blades/rotor, transient solvers provide a range of  $C_p$  values, which in the present case is for one complete revolution of the multibladed VAWT. As mentioned earlier, the transient performance characteristics of multibladed VAWT considered here have been reported previously by the authors as well [12,14]. However, those analyses were for system-level performance. In line with the aim of the present study, the transient aerodynamic performance of individual blades is being reported for the first time here. Figure 6a depicts the variations in  $C_p$  of the multibladed VAWT at different  $\lambda$  values. Some general observations are that during one complete revolution of the rotor, (i) the  $C_p$  of the rotor changes quite significantly; (ii) a crest is followed by a trough and vice versa; (iii) as  $\lambda$  increases, variations in  $C_p$  also increase; and (iv) for  $\lambda$  above 0.6, the troughs are below  $C_p = 0$ . For  $\lambda = 0.1$ , the crest and trough  $C_p$  values are 9.9% and 7.4%, while at  $\lambda = 1$ , these are 25.4% and  $-61.1\%$ . The reason for higher peak  $C_p$  values at higher  $\lambda$  is understandable, i.e., the rotor is rotating faster for a given wind speed. An interesting observation here is the shifting of  $C_p$  curves upwards as  $\lambda$  increases from 0.1 to 0.3. From  $\lambda = 0.4$ –1.0, although the peak  $C_p$  values remain the same as for  $\lambda = 0.3$ , the crests keep on shifting below. This clearly indicates the reasons for the decrease in  $C_p$  after  $\lambda = 0.3$  i.e., the windward blades produce the same power as at  $\lambda = 0.3$ , and the leeward blades depict negative power.

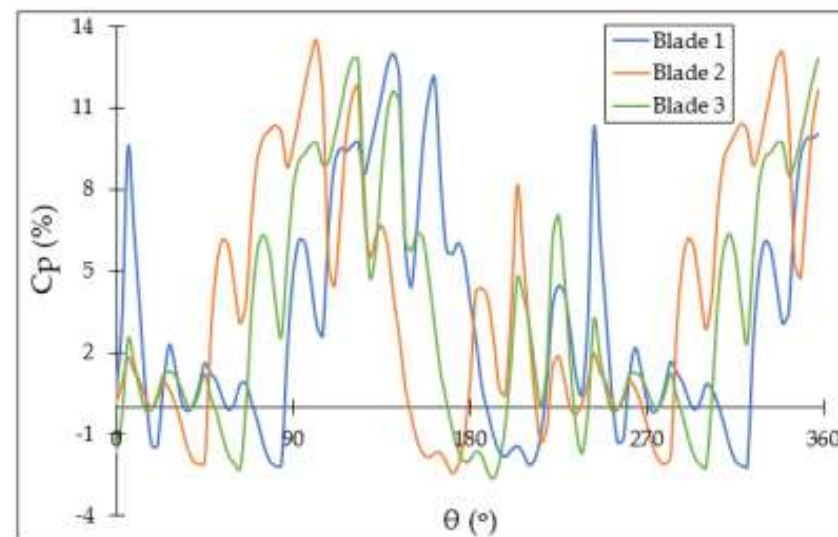


(a)

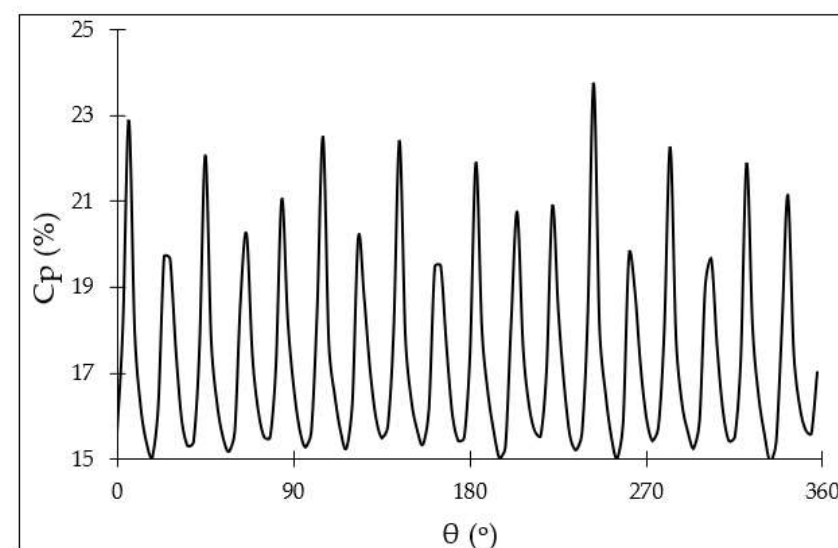
Figure 6. Cont.



(b)



(c)



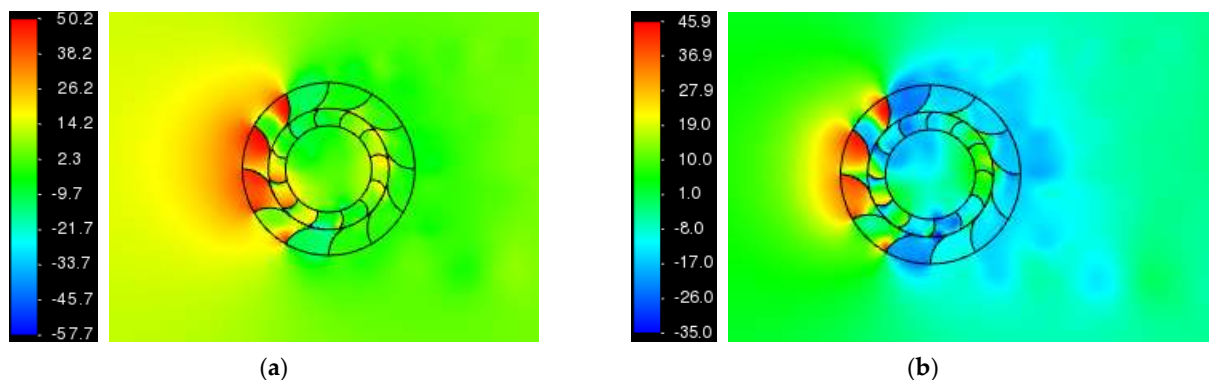
(d)

**Figure 6.** Transient  $C_p$  variations for multiblated VAWT (a) at different  $\theta$ ; (b) comparison with steady-state  $C_p$  (c) for each blade; (d) resultant of the VAWT at  $\lambda = 0.3$ .



Comparing the multibladed VAWT's  $C_p$  from steady-state and transient solvers, it can be seen in Figure 6b that the revolution-averaged  $C_p$  of the VAWT is slightly lower than steady-state  $C_p$  till  $\lambda = 0.5$ . After this  $\lambda$ , there is a sharp drop in steady-state  $C_p$  while there is a more gradual drop in revolution-averaged transient  $C_p$ . While the steady-state  $C_p$  drops below 0% at  $\lambda = 0.65$ , transient  $C_p$  drops below 0% at  $\lambda = 0.75$ . Thus, the operational range of the multibladed VAWT predicted by the transient solver is wider. Moreover, at  $\lambda = 1.0$ , the revolution-averaged transient  $C_p$  is  $-25\%$ , compared to  $-48\%$  predicted by the steady-state solver. Figure 6c,d depict the variations in transient  $C_p$  of individual rotor blades and the resultant of the VAWT at  $\lambda = 0.3$ . For clearer representation, instantaneous  $C_p$ s of only three rotor blades are shown. It can be seen that the aerodynamic journey of each blade is the same. The blades mostly produce positive  $C_p$ . Figure 6d indicates that the net  $C_p$  of the rotor is always positive at  $\lambda = 0.3$ . The reason for net positive  $C_p$  produced by the blades of multibladed VAWT is down to the large number of blades in the VAWT. This clearly indicates that increasing the number of rotor blades increases the power output of the VAWT because the blades produce more positive  $C_p$ , or they come out of their negative  $C_p$  quickly, as they are being replaced by their immediate neighboring blade.

Figure 7a,b depict local static pressure variations in the vicinity of multibladed VAWT for crests and troughs in Figure 6d. It is evident from Figure 7a that when a crest in net  $C_p$  occurs, most of the rotor blades experience positive air pressure, while in the case of troughs in net  $C_p$ , many rotor blades, especially the ones at the top and bottom of the rotor, experience significant negative air pressure. It is evident from the discussions in this study regarding pressure variations that the instantaneous position of individual rotor blades dictates their  $C_p$  contributions, while negative  $C_p$  can be mitigated to some extent using a greater number of rotor blades.



**Figure 7.** Static pressure variations in the vicinity of multibladed VAWT at (a) net  $C_p$  crest and (b) net  $C_p$  trough.

## 5. Conclusions

Numerical investigations on the power generating capability of a multibladed drag-based VAWT, comprising 12 rotor blades, were carried out in this study using advanced computational fluid dynamics (CFD) techniques, employing a sliding mesh solver. Comparison with the steady-state  $C_p$  and experimental data reveal that the revolution-averaged transient  $C_p$  values are closer to the experimentally recorded  $C_p$  values. The transient solver was shown to increase  $C_p$  prediction accuracy by 13%. Numerically predicted transient  $C_p$  of the multibladed VAWT provides a detailed description of the time-history of individual rotor blades during one complete revolution of the VAWT. The results obtained indicate that as  $\lambda$  increases beyond peak  $C_p$ , crests  $C_p$  of the VAWT remain the same; however, the trough  $C_p$  of the VAWT decreases, demonstrating that the  $C_p$  of the leeward rotor blades falls below 0%. At peak net  $C_p$ , individual blades of the rotor produce positive  $C_p$  for the majority of the rotation, while the net  $C_p$  of the rotor is always positive. This occurs because the negative  $C_p$  of an individual blade is compensated by the positive  $C_p$  of the neighboring blades. Net  $C_p$  crest flow diagnostics depict that most of the rotor blades

experience positive air pressure, while net  $C_p$  trough is associated with significant negative pressure at most of the rotor blades.

**Author Contributions:** Conceptualization, T.A. and S.Z.I.; methodology, T.A., J.C., T.L. and D.S.; formal analysis, T.A., J.C., T.L. and D.S.; investigation, T.A., J.C. and T.L.; resources, T.A. and S.Z.I.; data curation, T.A. and D.S.; writing—original draft preparation, T.A., J.C., T.L. and D.S.; writing—review and editing, S.Z.I. and M.S.S.; supervision, T.A., S.Z.I. and M.S.S. All authors have read and agreed to the published version of the manuscript.

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