

Supplementary File

Manuscript Title: Shared Mobility Problems: A Systematic Review on Types, Variants, Characteristics, and Solution Approaches

Table S1. Summary of Papers based on the Types of SMP

Paper	Ridesharing	Carpooling	Taxisharing	Buspooling	Vanpooling	Multi-Modal
Agatz et al. (2011)	✓					
Aissat and Oulamara (2014a)	✓					
Aissat and Oulamara (2014b)	✓					
Aissat and Oulamara (2015a)	✓					
Aissat and Oulamara (2015b)	✓					
Aissat and Oulamara (2015c)	✓					
Alonso-Mora et al. (2017)	✓					
Armant and Brown (2014)	✓					
Armant and Brown (2020)	✓					
Auad and Van Hentenryck (2021)						✓
Aydin et al. (2020)	✓					
Ben Cheikh et al. (2017)	✓					
Bian and Liu (2017)	✓					
Bian and Liu (2019a)	✓					
Bian and Liu (2019b)	✓					
Bit-Monnot et al. (2013)		✓				
Bruck et al. (2017)		✓				
Cangialosi et al. (2016)						✓
Cao et al. (2021)	✓					
Cheikh & Hammadi (2016)	✓					
Cheikh-Graiet et al. (2020)	✓					
Chen et al. (2019a)	✓					
Chen et al. (2019b)			✓			
Chen et al. (2019c)	✓					
Chou et al. (2016)		✓				
Di Febbraro et al. (2013)	✓					
Du et al. (2016)			✓			
Duan et al. (2018)		✓				
Enzi et al. (2020)						✓
Guan et al. (2020)	✓					

Guo et al. (2013)		✓			
Herbawi and Weber (2011a)	✓				
Herbawi and Weber (2011b)	✓				
Herbawi and Weber (2011c)	✓				
Herbawi and Weber (2012a)	✓				
Herbawi and Weber (2012b)	✓				
Herbawi and Weber (2012c)	✓				
Herbawi and Weber (2012d)	✓				
Hosni et al. (2014)			✓		
Hou et al. (2018)	✓				
Hsieh and Zhan (2018)		✓			
Hsieh et al. (2019)		✓			
Huang et al. (2014a)		✓			
Huang et al. (2014b)		✓			
Huang et al. (2016)		✓			
Huang et al. (2017)		✓			
Huang et al. (2018a)		✓			
Huang et al. (2018b)					✓
Jung et al. (2016)			✓		
Kaan and Olinick (2013)				✓	
Lee and Savelsbergh (2015)	✓				
Li and Chung (2020)	✓				
Li et al. (2018)	✓				
Lin et al. (2012)			✓		
Liu and Liu (2020)				✓	
Liu et al. (2019)				✓	
Lloret-Battle et al. (2017)	✓				
Long et al. (2018)	✓				
Lotfi et al. (2019)	✓				
Lu et al. (2020)	✓				
Ma (2017)					✓
Ma et al. (2018a)	✓				
Ma et al. (2018b)			✓		
Masoud and Jayakrishnan (2017a)	✓				
Masoud and Jayakrishnan (2017b)	✓				
Masoud et al. (2017a)					✓
Masoud et al. (2017b)	✓				

Massobrio et al. (2016)			✓			
Najmi et al. (2017)	✓					
Nam et al. (2018)						✓
Naoum-Sawaya et al. (2015)	✓					
Pelzer et al. (2015)	✓					
Qian et al. (2017)			✓			
Regue et al. (2016)						✓
Ren et al. (2020)	✓					
Santos and Xavier (2013)			✓			
Santos and Xavier (2015)			✓			
Simonetto et al. (2019)	✓					
Smet (2019)	✓					
Stiglic et al. (2015)	✓					
Stiglic et al. (2016)	✓					
Stiglic et al. (2018)						✓
Su et al. (2019)		✓				
Sun and Zhang (2018)			✓			
Tafreshian and Masoud (2020a)	✓					
Tafreshian and Masoud (2020b)	✓					
Tamannaei & Irandoost (2019)		✓				
Wang et al. (2018)	✓					
Wang et al. (2016)	✓					
Wu et al. (2016)		✓				
Xia et al. (2015)		✓				
Yan and Chen (2011a)		✓				
Yan and Chen (2011b)		✓				
Yan et al. (2011)		✓				
Yan et al. (2012)		✓				
Yan et al. (2014)		✓				
Ye et al. (2015)			✓			
Yu et al. (2019)	✓					
Yu et al. (2020)						✓
Zhang and Zhang (2020)	✓					
Zhang et al. (2019)	✓					
Zhang et al. (2020)			✓			
Zhao et al. (2018)	✓					

Table S2. Summary of Papers based on the Problem Variants of SMP

Paper	Riders and Drivers				Origins and Destinations			
	1-1	1-M	M-1	M-M	MO1D	1OMD	MOMD	1O1D
Agatz et al. (2011)	✓							
Aissat and Oulamara (2014b)	✓							
Aissat and Oulamara (2014a)	✓							
Aissat and Oulamara (2015a)	✓							
Aissat and Oulamara (2015b)	✓							
Aissat and Oulamara (2015c)	✓							
Alonso-Mora et al. (2017)		✓						
Armant and Brown (2014)		✓						
Armant and Brown (2020)		✓						
Aydin et al. (2020)	✓							
Ben Cheikh et al. (2017)				✓				
Bian and Liu (2017)		✓						
Bian and Liu (2019a)		✓						
Bian and Liu (2019b)		✓						
Bit-Monnot et al. (2013)		✓						
Bruck et al. (2017)	✓							
Cao et al. (2021)		✓						
Cheikh-Graiet et al. (2020)				✓				
Cheikh & Hammadi (2016)			✓					
Chen et al. (2019a)				✓				

Chen et al. (2019b)							✓	
Chen et al. (2019c)		✓						
Chou et al. (2016)			✓					
Di Febbraro et al. (2013)		✓						
Du et al. (2016)	✓							
Duan et al. (2018)	✓							
Guan et al. (2020)	✓							
Guo et al. (2013)						✓		
Herbawi and Weber (2011c)			✓					
Herbawi and Weber (2011b)		✓						
Herbawi and Weber (2011a)		✓						
Herbawi and Weber (2012d)		✓						
Herbawi and Weber (2012b)			✓					
Herbawi and Weber (2012a)		✓						
Herbawi and Weber (2012c)				✓				
Hosni et al. (2014)		✓						
Hou et al. (2018)		✓						
Hsieh and Zhan (2018)	✓							
Hsieh et al. (2019)		✓						
Huang et al. (2014a)		✓						
Huang et al. (2014b)		✓						
Huang et al. (2016)					✓			
Huang et al. (2017)		✓						
Huang et al. (2018a)		✓						
Jung et al. (2016)		✓						
Kaan and Olinick (2013)		✓						
Lee and Savelsbergh (2015)	✓							
Li and Chung (2020)				✓				
Li et al. (2018)		✓						
Lin et al. (2012)		✓						

Liu and Liu (2020)	✓							
Liu et al. (2019)		✓						
Lloret-Batlle et al. (2017)	✓							
Long et al. (2018)	✓							
Lotfi et al. (2019)				✓				
Lu et al. (2020)				✓				
Ma et al. (2018a)		✓						
Ma et al. (2018b)		✓						
Masoud and Jayakrishnan (2017a)				✓				
Masoud and Jayakrishnan (2017b)			✓	✓				
Masoud et al. (2017b)	✓	✓		✓				
Massobrio et al. (2016)						✓		
Najmi et al. (2017)	✓							
Naoum-Sawaya et al. (2015)	✓							
Pelzer et al. (2015)	✓							
Qian et al. (2017)	✓							
Ren et al. (2020)		✓						
Santos and Xavier (2013)				✓				
Santos and Xavier (2015)				✓				
Simonetto et al. (2019)	✓	✓						
Stiglic et al. (2015)		✓						
Stiglic et al. (2016)	✓							
Smet (2019)							✓	
Su et al. (2019)					✓			
Sun and Zhang (2018)		✓						
Tafreshian and Masoud (2020a)	✓	✓						
Tafreshian and Masoud (2020b)	✓							
Tamannaeei & Irandoost (2019)		✓						
Wang et al. (2018)	✓							
Wang et al. (2016)		✓						

Wu et al. (2016)	✓							
Xia et al. (2015)		✓						
Yan et al. (2012)							✓	
Yan et al. (2011)							✓	
Yan et al. (2014)							✓	
Yan and Chen (2011b)							✓	
Yan and Chen (2011a)							✓	
Ye et al. (2015)		✓						
Yu et al. (2019)		✓						
Zhang and Zhang (2020)	✓							
Zhang et al. (2019)		✓						
Zhang et al. (2020)		✓						
Zhao et al. (2018)		✓						

Table S3. Summary of Papers based on the Characteristics of SMP

Paper	Problem Characteristics												Data Characteristics				
	DC	MO	MH	RB	TP	TW	MP	ROF	ROUF	ATF	TF	DDF	PDF	SB	STA	STO	Dy
Agatz et al. (2011)				✓				✓									✓
Aissat and Oulamara (2014b)						✓	✓										✓
Aissat and Oulamara (2014a)						✓	✓										✓
Aissat and Oulamara (2015a)						✓	✓										✓
Aissat and Oulamara (2015b)						✓	✓										✓
Aissat and Oulamara (2015c)				✓		✓	✓										✓
Alonso-Mora et al. (2017)						✓											✓
Armant and Brown (2014)						✓		✓									✓
Armant and Brown (2020)		✓				✓		✓									✓
Aquad and Van Hentenryck (2021)		✓			✓	✓											✓
Aydin et al. (2020)							✓										✓
Ben Cheikh et al. (2017)		✓	✓		✓	✓											✓
Bian and Liu (2017)															✓		
Bian and Liu (2019a)		✓													✓		
Bian and Liu (2019b)		✓													✓		

Herbawi and Weber (2012b)		✓	✓															✓
Herbawi and Weber (2012a)		✓				✓			✓			✓						✓
Herbawi and Weber (2012c)		✓	✓		✓	✓						✓			✓			
Hosni et al. (2014)	✓					✓									✓			✓
Hou et al. (2018)	✓					✓									✓			
Hsieh and Zhan (2018)															✓			
Hsieh et al. (2019)	✓														✓			
Huang et al. (2014a)		✓													✓			
Huang et al. (2014b)		✓													✓			
Huang et al. (2016)															✓			
Huang et al. (2017)		✓													✓			
Huang et al. (2018a)		✓				✓									✓			
Huang et al. (2018b)			✓		✓										✓			
Jung et al. (2016)		✓				✓												✓
Kaan and Olinick (2013)						✓									✓			
Lee and Savelsbergh (2015)						✓				✓								✓
Li and Chung (2020)	✓					✓									✓			
Li et al. (2018)						✓	✓								✓			
Lin et al. (2012)		✓				✓									✓			
Liu and Liu (2020)	✓	✓													✓			

Herbawi and Weber (2011b)	✓	✓	✓															
Herbawi and Weber (2011a)	✓	✓	✓															
Herbawi and Weber (2012d)	✓			✓								✓						
Herbawi and Weber (2012b)	✓	✓	✓															
Herbawi and Weber (2012a)	✓			✓								✓						
Herbawi and Weber (2012c)	✓			✓								✓						
Hosni et al. (2014)													✓					
Hou et al. (2018)																	✓	
Hsieh and Zhan (2018)			✓															
Hsieh et al. (2019)			✓															
Huang et al. (2014a)			✓	✓	✓							✓		✓				
Huang et al. (2014b)			✓						✓									
Huang et al. (2016)			✓															
Huang et al. (2017)			✓	✓								✓					✓	

Huang et al. (2018a)				✓										✓			✓		
Huang et al. (2018b)			✓																
Jung et al. (2016)			✓												✓				
Kaan and Olinick (2013)			✓																
Lee and Savelsbergh (2015)			.											✓					
Li and Chung (2020)			✓																
Li et al. (2018)			✓																
Lin et al. (2012)	✓		✓																
Liu and Liu (2020)				✓										✓					
Liu et al. (2019)				✓															
Lloret-Batlle et al. (2017)			✓																
Long et al. (2018)	✓		✓					✓						✓					
Lotfi et al. (2019)															✓				
Lu et al. (2020)			✓																
Ma (2017)	✓																		
Ma et al. (2018a)			✓																
Ma et al. (2018b)	✓			✓															
Masoud and Jayakrishnan (2017a)														✓					

Zhang and Zhang (2020)			✓																✓	
Zhang et al. (2019)				✓																
Zhang et al. (2020)				✓									✓							
Zhao et al. (2018)			✓							✓										

Table S5: List of Algorithms employed in selected Papers for SMP

Paper	Algorithms / Approaches
Agatz et al. (2011)	Greedy matching algorithm
Aissat and Oulamara (2014a)	Bidirectional search algorithm + shortest path one-to-all (heuristic)
Aissat and Oulamara (2014b)	Enumerative method (exact) + heuristic with closest nodes metric + heuristic with global path's total cost metric
Aissat and Oulamara (2015a)	Bidirectional search algorithm + shortest path one-to-all (heuristic)
Aissat and Oulamara (2015b)	Bidirectional search algorithm + shortest path one-to-all (heuristic)
Aissat and Oulamara (2015c)	Improved Dijkstra algorithm with the concept of adding offer and demand
Alonso-Mora et al. (2017)	Greedy assignment + constrained optimization
Armant and Brown (2014)	CPLEX
Armant and Brown (2020)	CPLEX
Auad and Van Hentenryck (2021)	Route enumeration algorithm + fleet sizing algorithm
Aydin et al. (2020)	Heuristic + Needleman-Wunsch algorithm
Ben Cheikh et al. (2017)	Metaheuristic Approach Based on Controlled Genetic Operators (MACGeO)
Bian and Liu (2017)	Simulated annealing with four neighbourhood structure

Bian and Liu (2019a)	Solution Pooling Approach (SPA)
Bian and Liu (2019b)	Solution Pooling Approach (SPA)
Bit-Monnot et al. (2013)	Exact and heuristic dominance rule
Bruck et al. (2017)	Greedy constructive heuristic + refined based local search (two-stage algorithm)
Cangialosi et al. (2016)	MILP solver
Cao et al. (2021)	Genetic algorithm
Cheikh & Hammadi (2016)	Autonomous and Intelligent Agents
Cheikh-Graiet et al. (2020)	Multi-criterion tabu search algorithm
Chen et al. (2019a)	Greedy heuristic
Chen et al. (2019b)	Rollover approach + local search
Chen et al. (2019c)	Cluster-based solution method
Chou et al. (2016)	Stochastic set based particle swarm optimization
Di Febbraro et al. (2013)	Discrete event systems based simulation
Du et al. (2016)	LINGO
Duan et al. (2018)	Partition merging based on greedy algorithms
Enzi et al. (2020)	Column generation based algorithm
Guan et al. (2020)	Hybrid VNS-NSGA-II algorithm
Guo et al. (2013)	Hybrid ant colony algorithm
Herbawi and Weber (2011a)	Non-Dominated Sorting Genetic Algorithm II (NSGA-II) + multi-objective ant colony optimization
Herbawi and Weber (2011b)	Non-Dominated Sorting Genetic Algorithm II (NSGA-II) + Improved Strength Pareto Evolutionary Algorithm (SPEA2) + Region-based Selection in Evolutionary Multiobjective Optimization (PESA-II) + Indicator-Based Selection in Multiobjective Search (IBEA)
Herbawi and Weber (2011c)	Non-Dominated Sorting Genetic Algorithm II (NSGA-II)
Herbawi and Weber (2012a)	Genetic and insertion heuristic algorithm
Herbawi and Weber (2012b)	Genetic local search algorithm

Herbawi and Weber (2012c)	Genetic algorithm
Herbawi and Weber (2012d)	Genetic algorithm
Hosni et al. (2014)	Simple heuristic, incremental cost heuristic (ICH) with Lagrangian decomposition approach
Hou et al. (2018)	Large neighbourhood search algorithm
Hsieh and Zhan (2018)	Differential evolution
Hsieh et al. (2019)	Discrete cooperative coevolving particle swarm optimization (DCCPSO) algorithm
Huang et al. (2014a)	Genetic algorithm
Huang et al. (2014b)	Fuzzy controlled genetic algorithm
Huang et al. (2016)	Tabu search
Huang et al. (2017)	Heuristic Multi-Objective Optimization Algorithm (HMOCSPHI) based on Non-Dominated Sorting Genetic Algorithm
Huang et al. (2018a)	Ant Path-oriented Carpooling Allocation (APCA) approach
Huang et al. (2018b)	Dijkstra Algorithm and A* Algorithm + concept of Drive-Time Areas (DTAs)
Jung et al. (2016)	Hybrid simulated annealing
Kaan and Olinick (2013)	Restricted allowance heuristic + relaxed restricted allowance heuristic + greedy cover heuristic
Lee and Savelsbergh (2015)	Path construction + neighbourhood search
Li and Chung (2020)	Hybrid heuristic algorithm based on an insertion algorithm and tabu search + clustering algorithm (greedy heuristic and k-means algorithm)
Li et al. (2018)	Tabu based metaheuristic algorithm
Lin et al. (2012)	Simulated annealing algorithm
Liu and Liu (2020)	Dynamic grid-based heuristic algorithm
Liu et al. (2019)	Exact algorithm and approximate algorithm
Lloret-Batlle et al. (2017)	VCG Mechanism + min-cost flow + network simplex
Long et al. (2018)	Monte carlo simulation
Lotfi et al. (2019)	Decomposition based modified column generation algorithm
Lu et al. (2020)	Lagrangian relaxation solution approach + two stage heuristic method

Ma (2017)	Shareability concept
Ma et al. (2018a)	Recursive algorithm + delete operator
Ma et al. (2018b)	improved genetic algorithm + banker principle + crowding density
Masoud and Jayakrishnan (2017a)	Decomposition algorithm
Masoud and Jayakrishnan (2017b)	Dynamic programming
Masoud et al. (2017a)	Dynamic programming
Masoud et al. (2017b)	Dynamic programming
Massobrio et al. (2016)	Non-Dominated Sorting Genetic Algorithm II (NSGA-II)
Najmi et al. (2017)	Clustering heuristic approach
Nam et al. (2018)	Dynamic programming
Naoum-Sawaya et al. (2015)	Savings heuristic
Pelzer et al. (2015)	Partition based algorithm
Qian et al. (2017)	Exact and heuristic for induced group ride graph
Regue et al. (2016)	Aggregation–disaggregation algorithm + decomposition approach
Ren et al. (2020)	Genetic algorithm
Santos and Xavier (2013)	Greedy Randomized Adaptive Search Procedure (GRASP)
Santos and Xavier (2015)	Greedy Randomized Adaptive Search Procedure (GRASP)
Simonetto et al. (2019)	Insertion heuristic + large neighbourhood search algorithm
Smet (2019)	Late acceptance hill climbing
Stiglic et al. (2015)	Basic algorithm + refined algorithm / hierarchical optimization approach
Stiglic et al. (2016)	Matching, schedule, detour flexibility + lexicographic optimization
Stiglic et al. (2018)	Ride-matching algorithm (match identification phase + optimization phase)
Su et al. (2019)	Artificial bee colony algorithm combining variable neighbour search and tabu list
Sun and Zhang (2018)	Insertion heuristic

Tafreshian and Masoud (2020a)	Graph partitioning algorithm based on the bipartite graph
Tafreshian and Masoud (2020b)	Decomposition algorithm based on Lagrangian relaxation
Tamannaee & Irandoost (2019)	Branch & bound + heuristic beam search algorithm
Wang et al. (2018)	Greedy matching method
Wang et al. (2016)	Tabu search + greedy insertion + adjust pickup time algorithm
Wu et al. (2016)	Local search (hill climbing, simulated annealing, swap and move neighbourhood, random neighbourhood) + exhaustive search (dynamic programming)
Xia et al. (2015)	Simulated annealing + tabu search
Yan and Chen (2011a)	Solution algorithm based on Lagrangian relaxation, a subgradient method, and a heuristic for the upper bound solution
Yan and Chen (2011b)	Solution algorithm based on Lagrangian relaxation, a subgradient method, and a heuristic for the upper bound solution
Yan et al. (2011)	Solution algorithm based on Lagrangian relaxation, a subgradient method, and a heuristic for the upper bound solution
Yan et al. (2012)	Solution algorithm based on Lagrangian relaxation, a subgradient method, and a heuristic for the upper bound solution
Yan et al. (2014)	Solution algorithm based on Lagrangian relaxation, a subgradient method, and a heuristic for the upper bound solution
Ye et al. (2015)	Non-Dominated Sorting Genetic Algorithm (NSGA)
Yu et al. (2019)	Decomposition method + exact algorithm
Yu et al. (2020)	Angle based clustering algorithm
Zhang and Zhang (2020)	Set-based differential evolution algorithm
Zhang et al. (2019)	Parallel scheme with simulated annealing
Zhang et al. (2020)	Improved genetic algorithm with station coding and decoding design.
Zhao et al. (2018)	Customized solution approach based on Lagrangian relaxation

Table S6: Summary of Papers based on the Solution Approaches of SMP

Paper	Exact	Heuristic / Metaheuristic	Others Approaches
Agatz et al. (2011)	✓		
Aissat and Oulamara (2014a)	✓	✓	
Aissat and Oulamara (2014b)	✓	✓	
Aissat and Oulamara (2015a)	✓	✓	
Aissat and Oulamara (2015b)	✓	✓	
Aissat and Oulamara (2015c)	✓		
Alonso-Mora et al. (2017)	✓	✓	
Armant and Brown (2014)	✓		
Armant and Brown (2020)	✓		
Auad and Van Hentenryck (2021)			✓
Aydin et al. (2020)		✓	
Ben Cheikh et al. (2017)		✓	
Bian and Liu (2017)		✓	
Bian and Liu (2019a)		✓	
Bian and Liu (2019b)		✓	
Bit-Monnot et al. (2013)	✓	✓	
Bruck et al. (2017)	✓	✓	
Cangialosi et al. (2016)	✓		
Cao et al. (2021)		✓	
Cheikh & Hammadi (2016)		✓	
Cheikh-Graiet et al. (2020)		✓	
Chen et al. (2019a)		✓	
Chen et al. (2019b)		✓	
Chen et al. (2019c)		✓	
Chou et al. (2016)		✓	
Di Febraro et al. (2013)			✓
Du et al. (2016)	✓		
Duan et al. (2018)		✓	
Enzi et al. (2020)	✓		
Guan et al. (2020)		✓	
Guo et al. (2013)		✓	

Herbawi and Weber (2011a)		✓	
Herbawi and Weber (2011b)		✓	
Herbawi and Weber (2011c)		✓	
Herbawi and Weber (2012a)		✓	
Herbawi and Weber (2012b)		✓	
Herbawi and Weber (2012c)		✓	
Herbawi and Weber (2012d)		✓	
Hosni et al. (2014)	✓	✓	
Hou et al. (2018)		✓	
Hsieh and Zhan (2018)		✓	
Hsieh et al. (2019)		✓	
Huang et al. (2014a)		✓	
Huang et al. (2014b)		✓	
Huang et al. (2016)		✓	
Huang et al. (2017)		✓	
Huang et al. (2018a)		✓	
Huang et al. (2018b)	✓		
Jung et al. (2016)		✓	
Kaan and Olinick (2013)		✓	
Lee and Savelsbergh (2015)		✓	
Li and Chung (2020)	✓	✓	
Li et al. (2018)		✓	
Lin et al. (2012)		✓	
Liu and Liu (2020)		✓	
Liu et al. (2019)	✓	✓	
Lloret-Batlle et al. (2017)			✓
Long et al. (2018)			✓
Lotfi et al. (2019)	✓		
Lu et al. (2020)		✓	
Ma (2017)			✓
Ma et al. (2018a)		✓	
Ma et al. (2018b)		✓	
Masoud and Jayakrishnan (2017a)	✓		

Masoud and Jayakrishnan (2017b)	✓		
Masoud et al. (2017a)	✓		
Masoud et al. (2017b)	✓		
Massobrio et al. (2016)			✓
Najmi et al. (2017)			✓
Nam et al. (2018)	✓		
Naoum-Sawaya et al. (2015)			✓
Pelzer et al. (2015)	✓		
Qian et al. (2017)	✓		✓
Regue et al. (2016)	✓		
Ren et al. (2020)			✓
Santos and Xavier (2013)			✓
Santos and Xavier (2015)			✓
Simonetto et al. (2019)			✓
Smet (2019)			✓
Stiglic et al. (2015)	✓		
Stiglic et al. (2016)	✓		
Stiglic et al. (2018)	✓		
Su et al. (2019)			✓
Sun and Zhang (2018)			✓
Tafreshian and Masoud (2020a)			✓
Tafreshian and Masoud (2020b)	✓		
Tamannaei & Irandoost (2019)	✓		✓
Wang et al. (2018)	✓		
Wang et al. (2016)			✓
Wu et al. (2016)			✓
Xia et al. (2015)			✓
Yan and Chen (2011a)			✓
Yan and Chen (2011b)			✓
Yan et al. (2011)			✓
Yan et al. (2012)			✓
Yan et al. (2014)			✓
Ye et al. (2015)			✓

Yu et al. (2019)	✓		
Yu et al. (2020)		✓	
Zhang and Zhang (2020)		✓	
Zhang et al. (2019)		✓	
Zhang et al. (2020)		✓	
Zhao et al. (2018)		✓	

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